



Introduction to Computer Graphics

7. Hidden Surface Removal & Culling

National Chiao Tung Univ, Taiwan

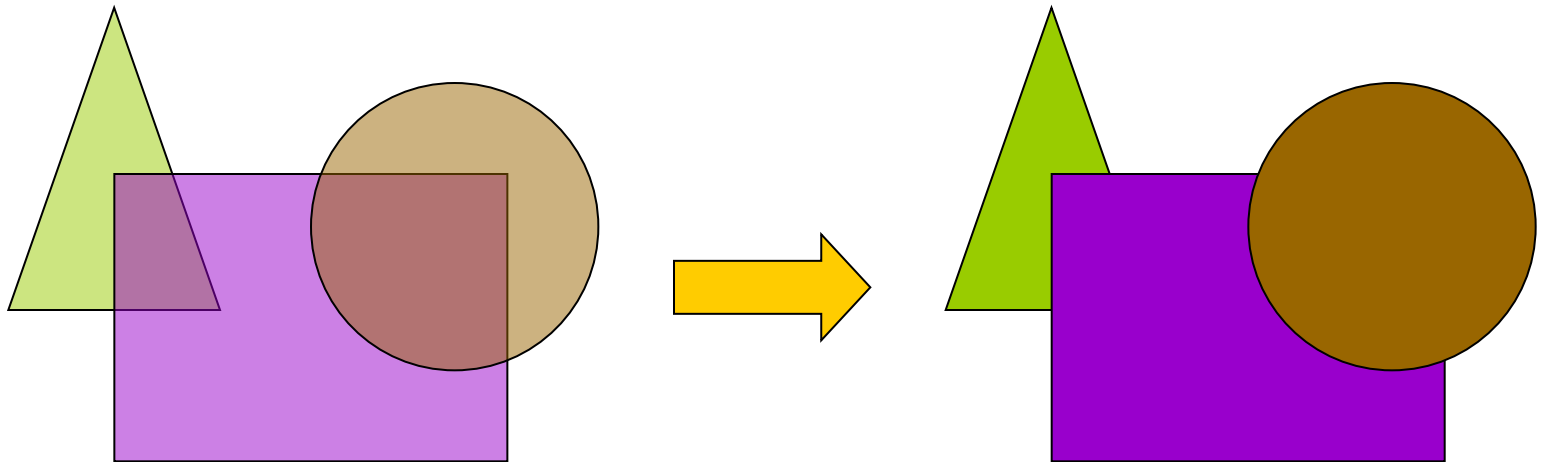
By: I-Chen Lin, Assistant Professor

Textbook: E. Angel, Interactive Computer Graphics, 5th Ed., Addison Wesley

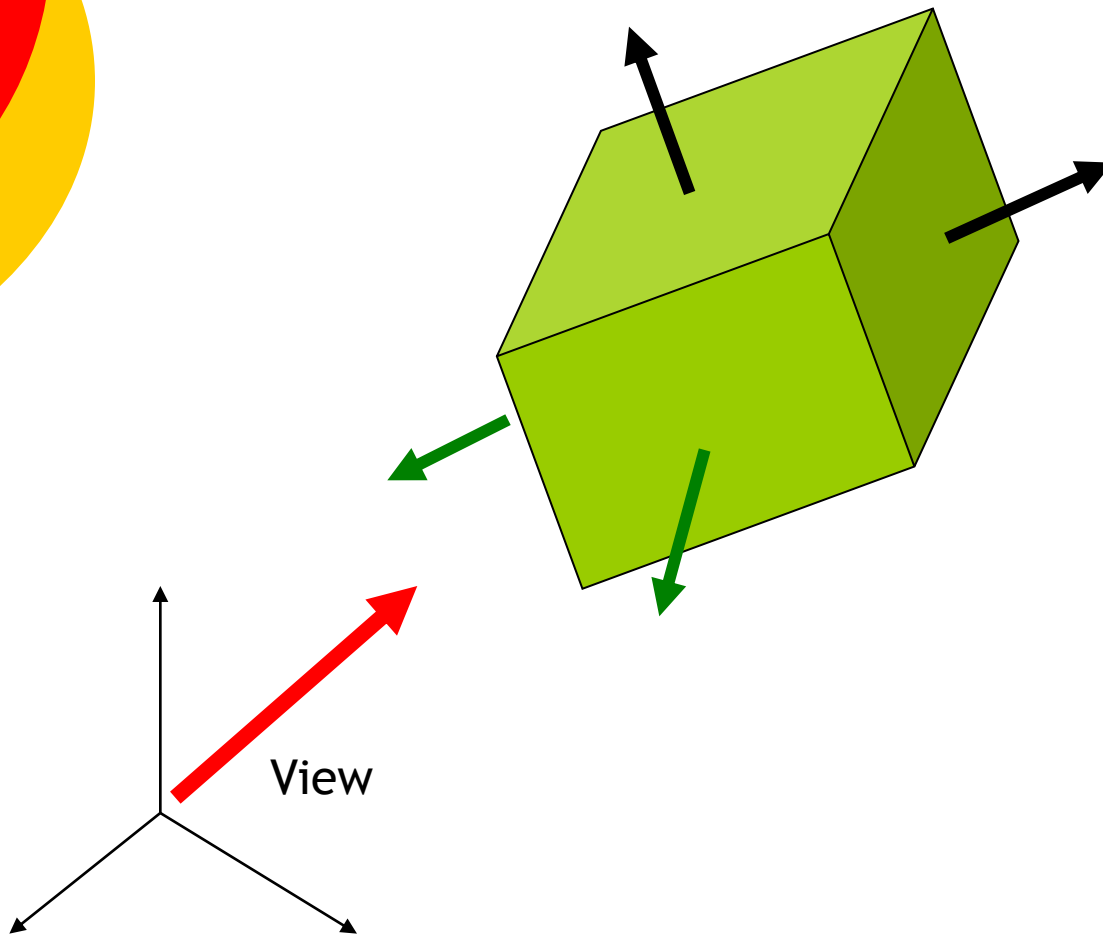
Ref: Hearn and Baker, Computer Graphics, 3rd Ed., Prentice Hall

Objectives

- In Hw1 (3D wireframe displayer), we can simply draw the line segments between projected point pairs.
- To fill projected polygons, we have to remove “hidden surfaces”.

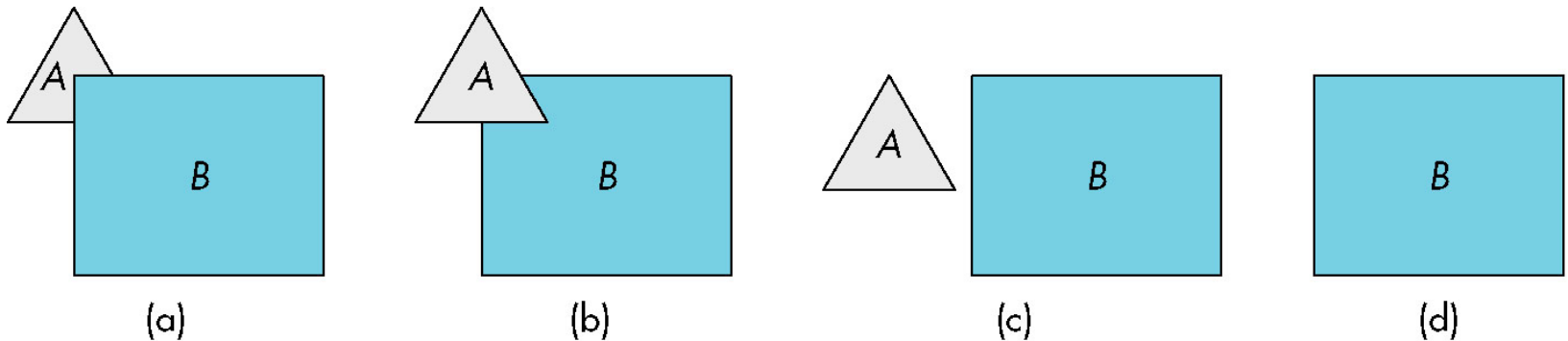


Backface Culling



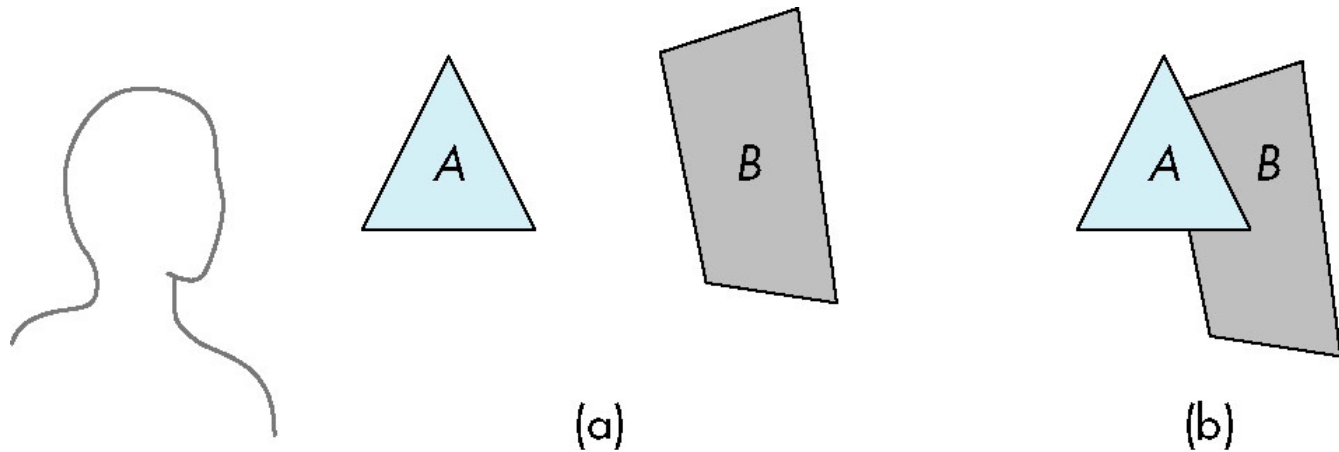
Hidden Surface Removal

- Object-space approach: use pairwise testing between polygons (objects)
- Worst case complexity $O(n^2)$ for n polygons



Painter's Algorithm

- Render polygons in a back to front order so that polygons behind others are simply painted over

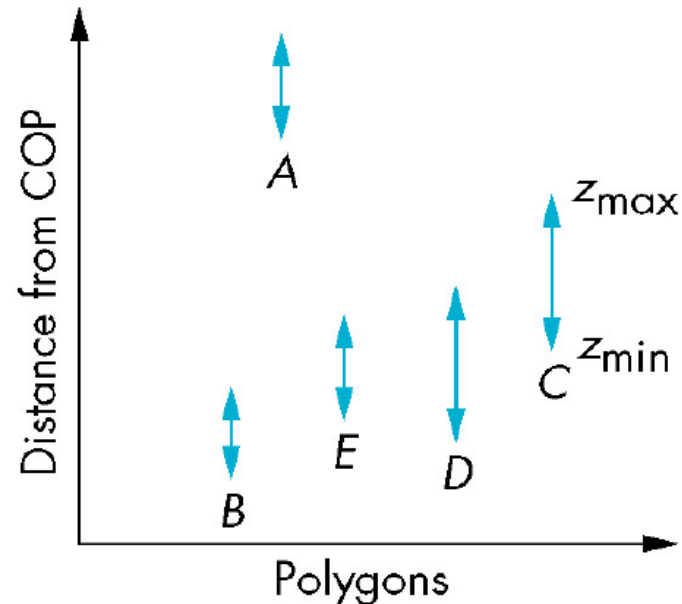


B behind A as seen by the viewer

Fill B then A

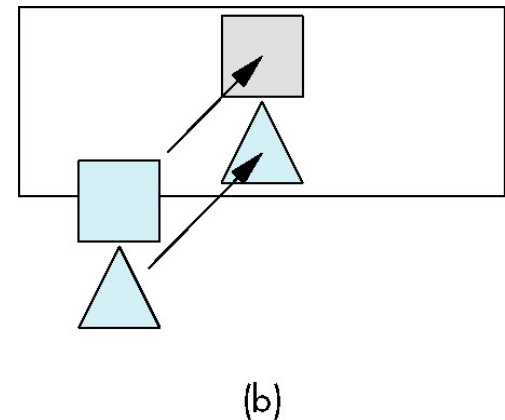
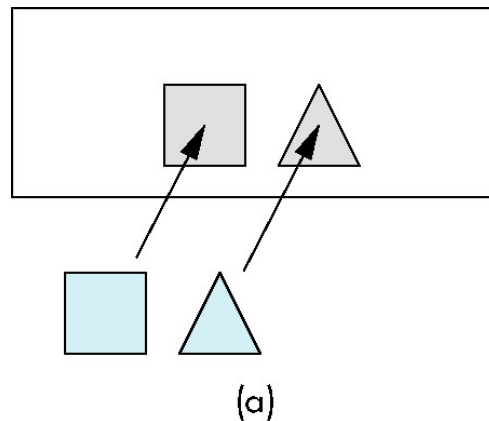
Depth Sort

- Requires ordering of polygons first
 - $O(n \log n)$ calculation for ordering
 - Not every polygon is either in front or behind all other polygons
- Order polygons and deal with easy cases first, harder later

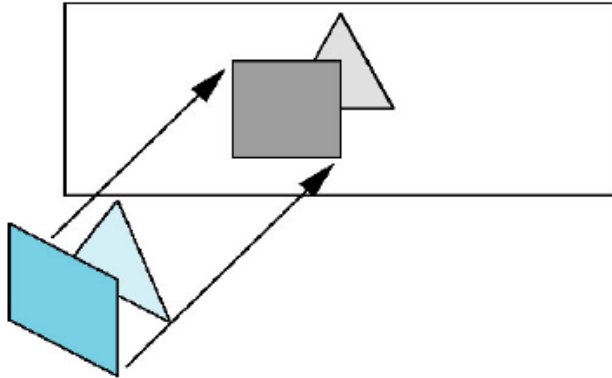


Easy Cases

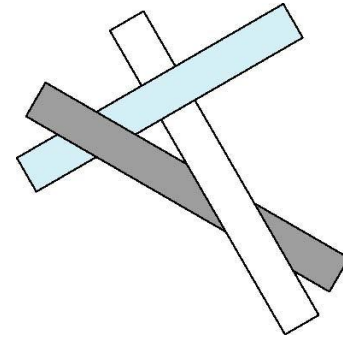
- A polygon lies behind all other polygons
 - Can render
- Polygons overlap in z but not in either x or y
 - Can render independently



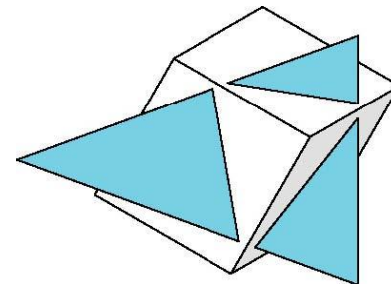
Difficult Cases



Overlap in all directions but
can one is fully on one side
of the other



cyclic overlap



penetration

Image Space Approach

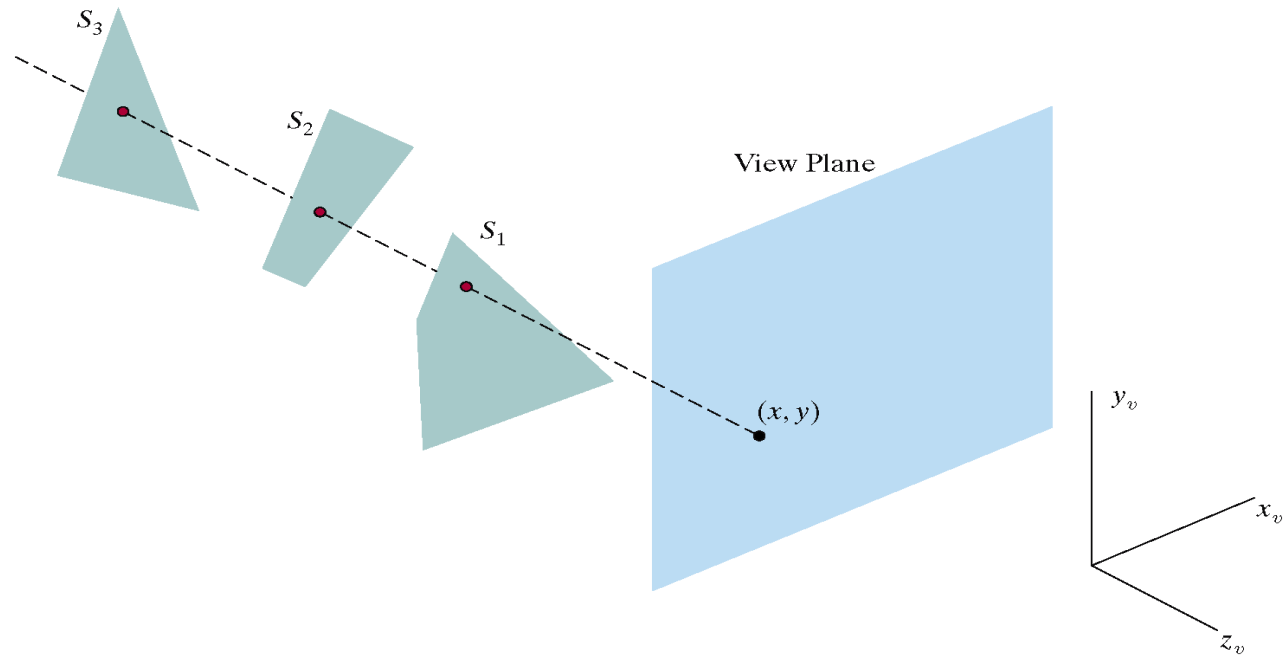
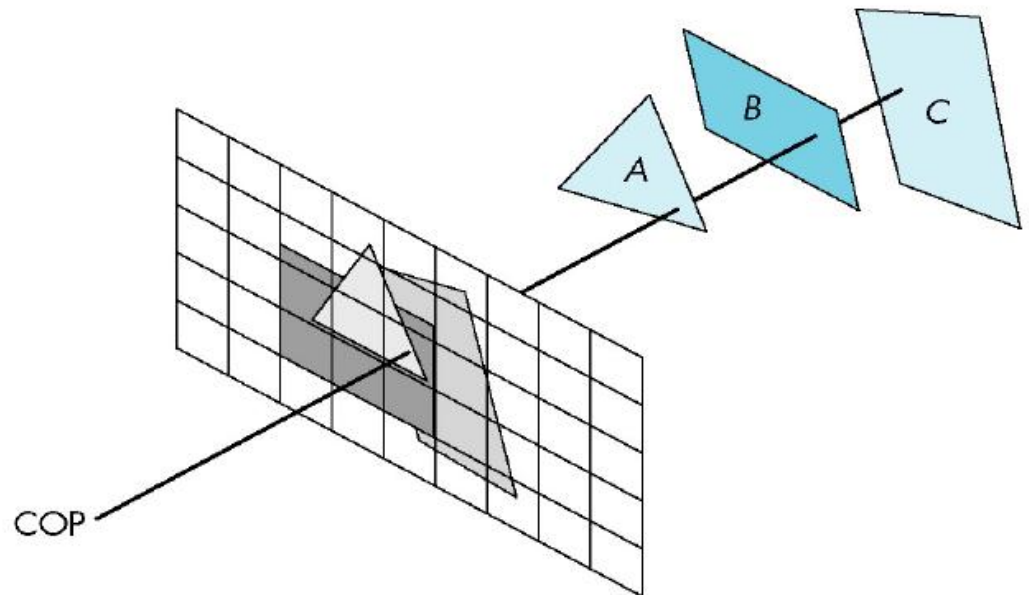


Figure 9-4

Three surfaces overlapping pixel position (x, y) on the view plane. The visible surface, S_1 , has the smallest depth value.

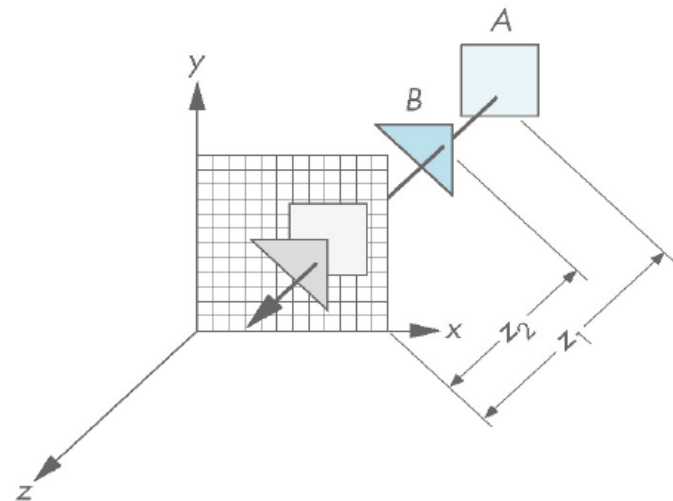
Image Space Approach

- Look at each projector (nm for an $n \times m$ frame buffer) and find closest of k polygons
- Complexity $O(nmk)$
- Ray casting
- z-buffer



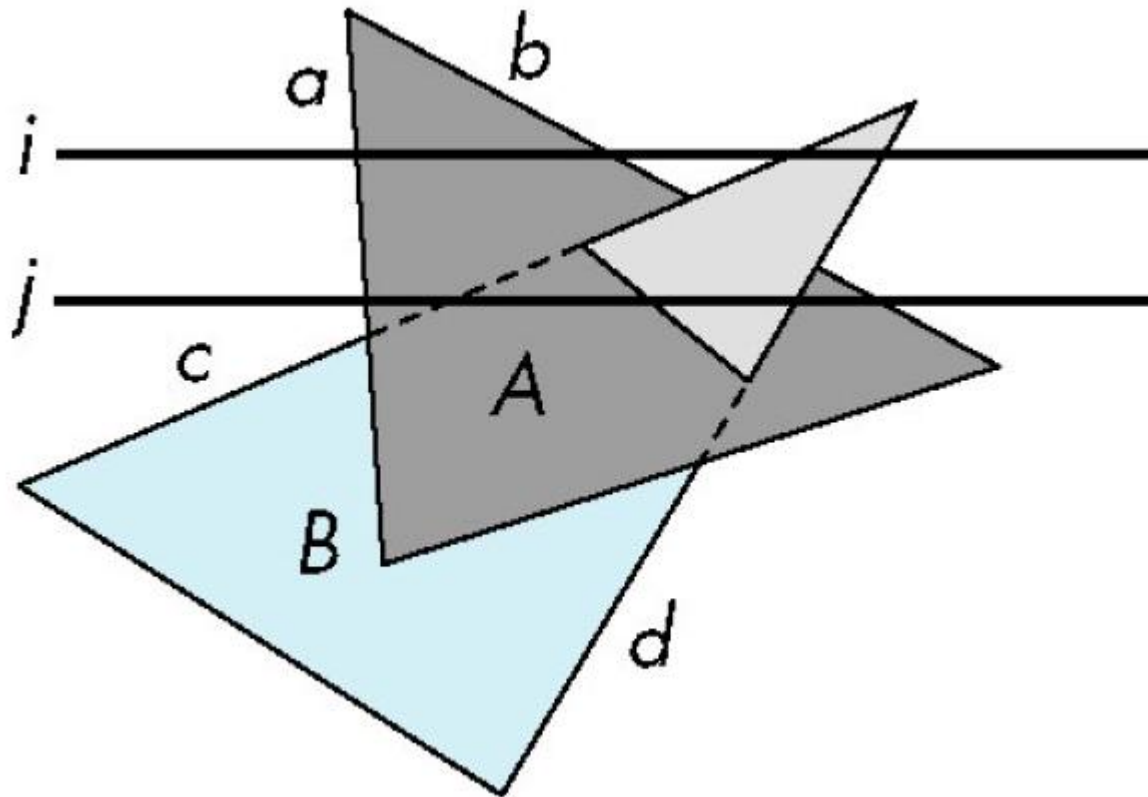
z-Buffer Algorithm

- The z or depth buffer
 - store the depth of the closest object at each pixel found so far
- As we render each polygon, compare the depth of each pixel to depth in z buffer
 - If less, place the shade of pixel in the color buffer and update z buffer

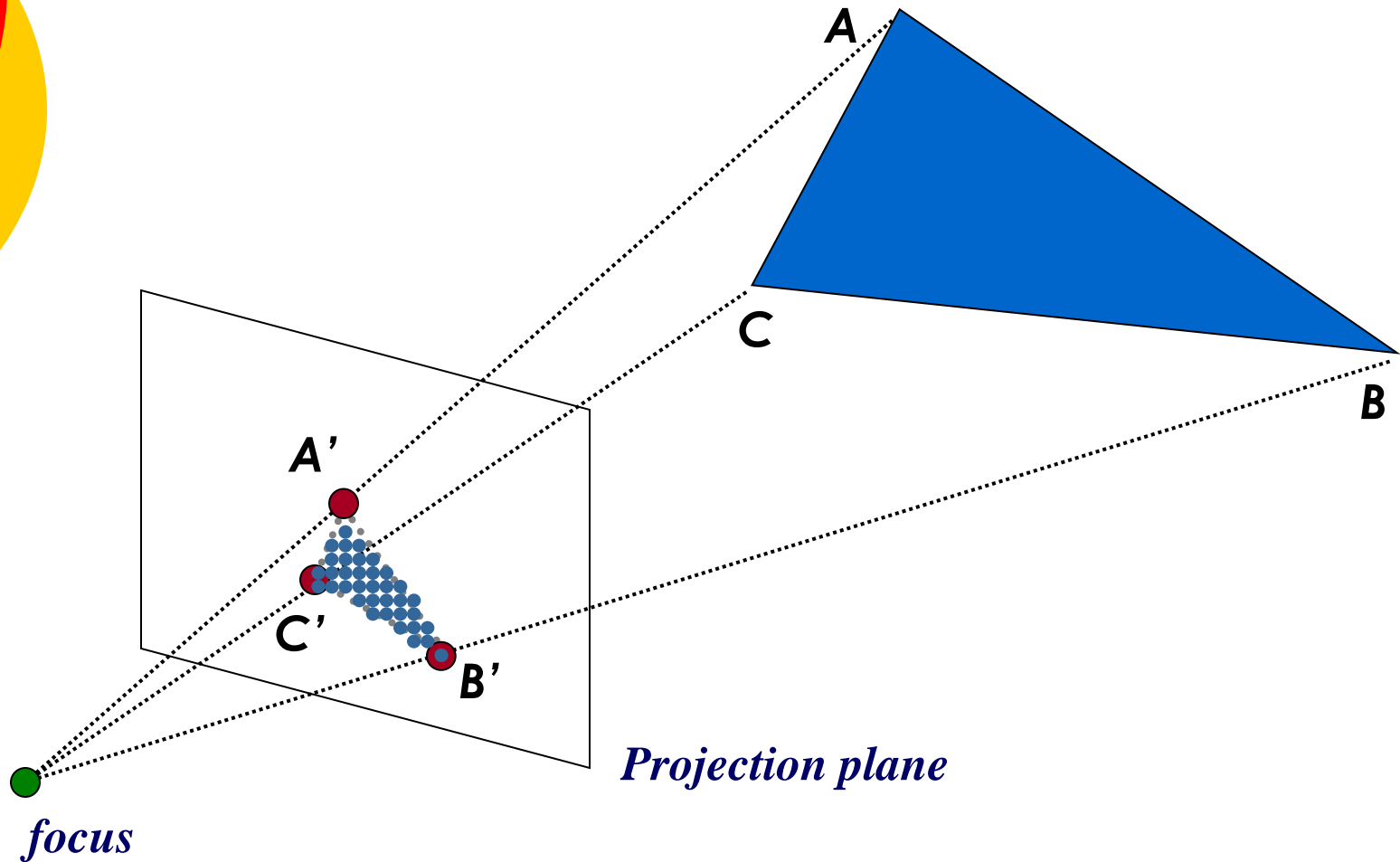


Scan-Line Algorithm

- Can combine shading and hsr through scan line algorithm

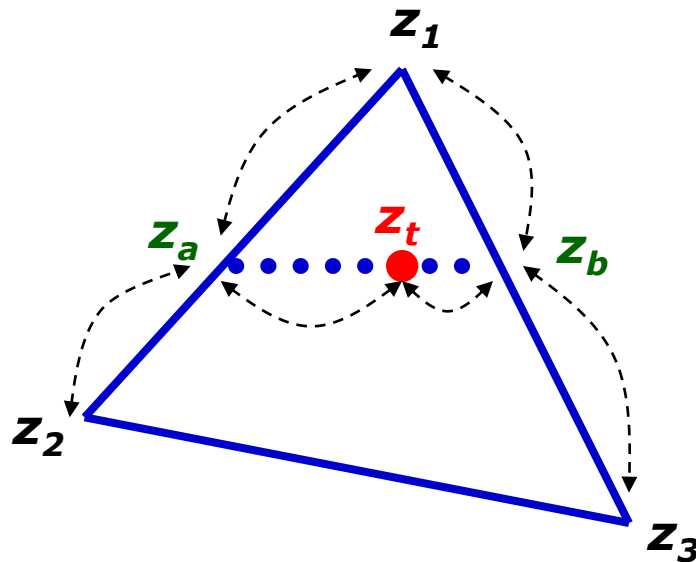


Interpolation of Z values



Interpolation of Z values

- To fill the polygon on the screen, we only fill the color and estimate the z value “pixel by pixel”.
- How to estimate z of in-between pixels ?



Screen Space vs. 3D Space

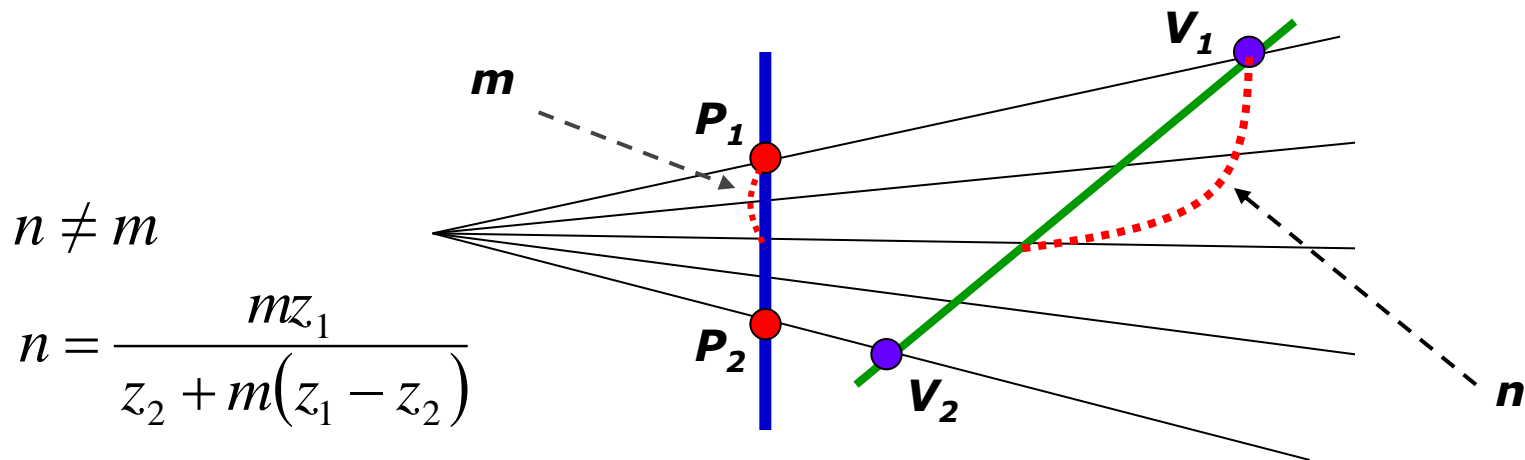
- Interpolation in screen space

- $P(m) = P_1 + m(P_2 - P_1)$

- Interpolation in 3D space

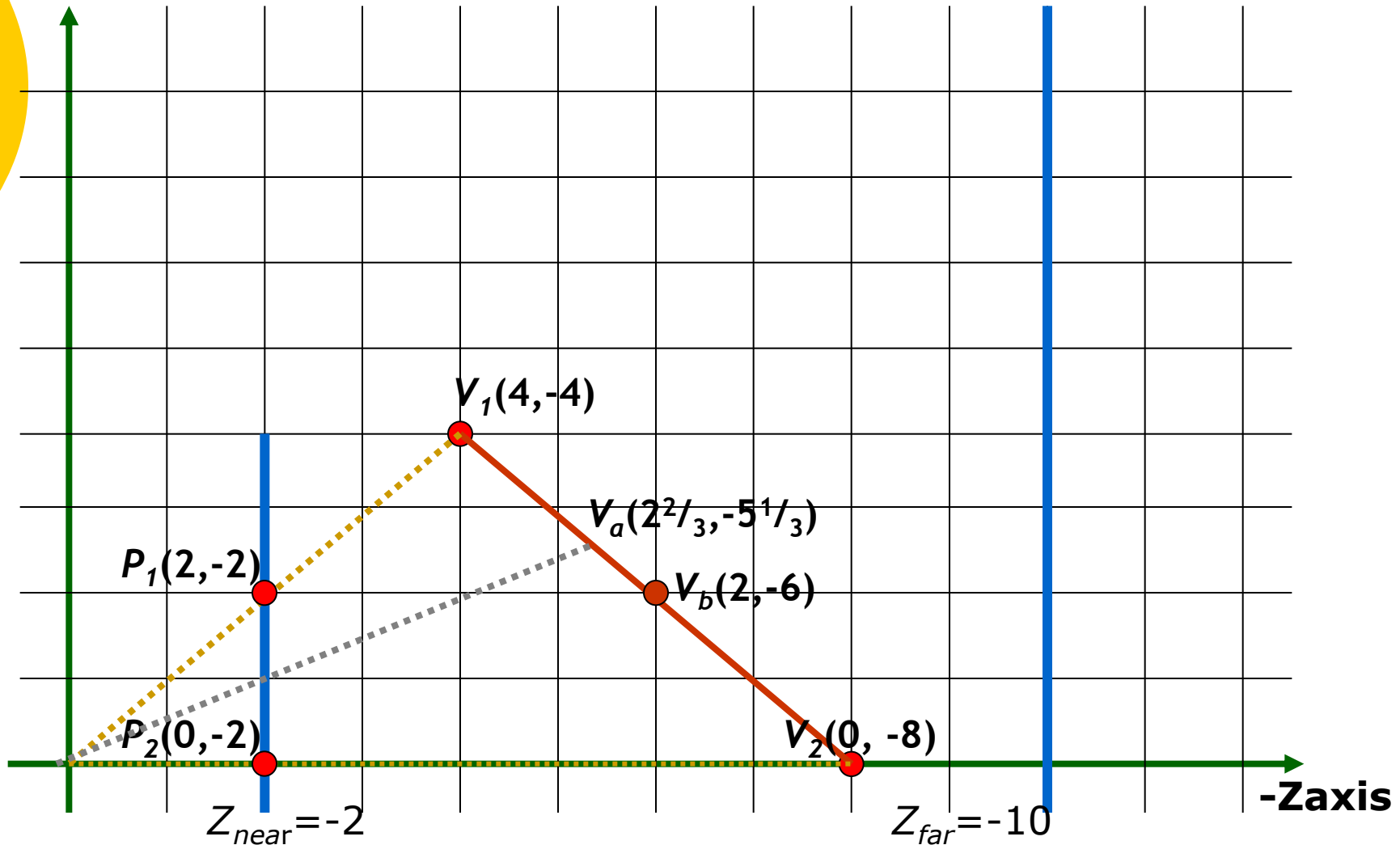
- $V(n) = V_1 + n(V_2 - V_1)$

- $P_y(n) = V_y(n) / V_z(n)$



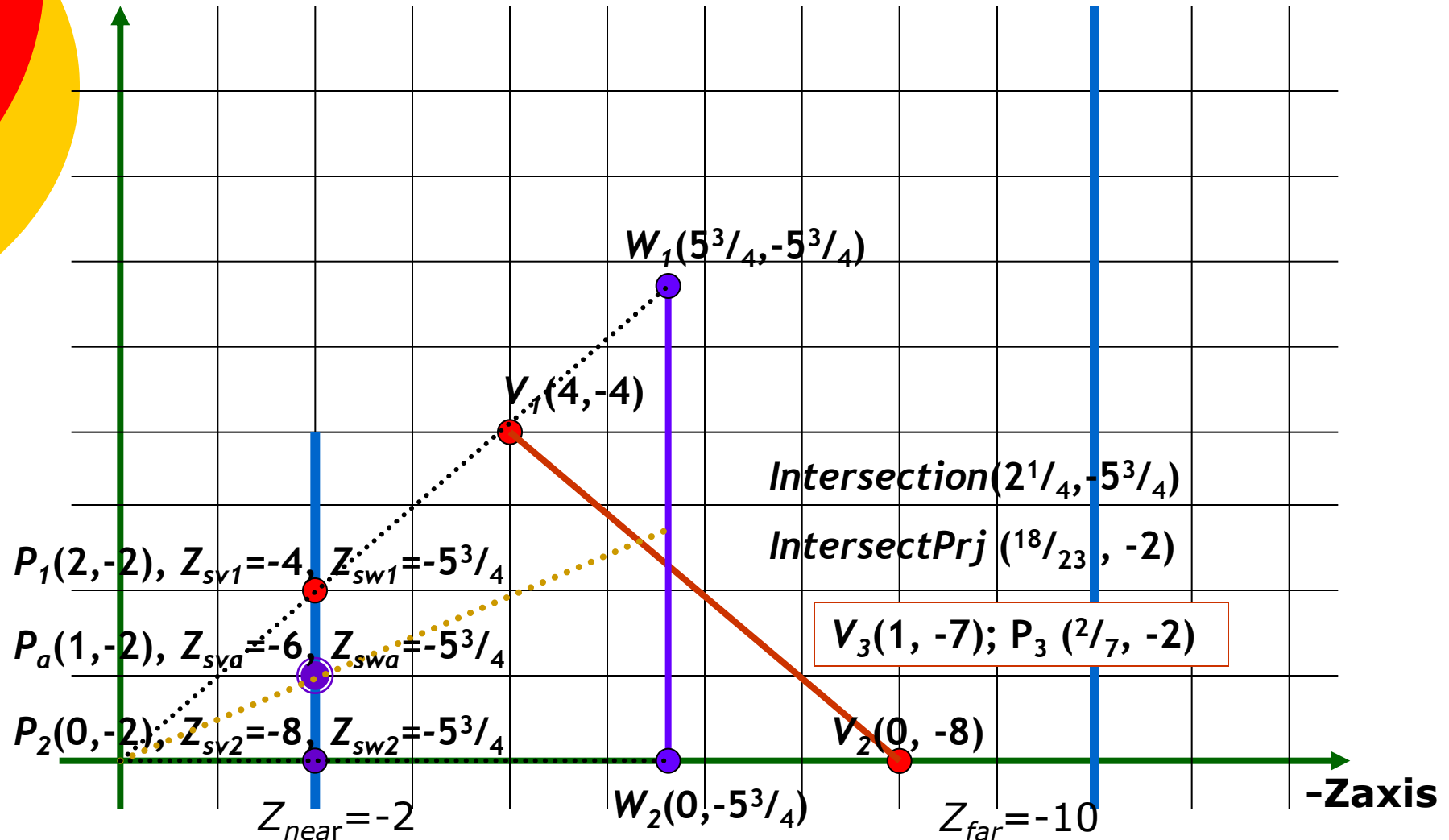
Screen Space vs. 3D Space

Y-axis



Simple Screen Interpolation

Y-axis



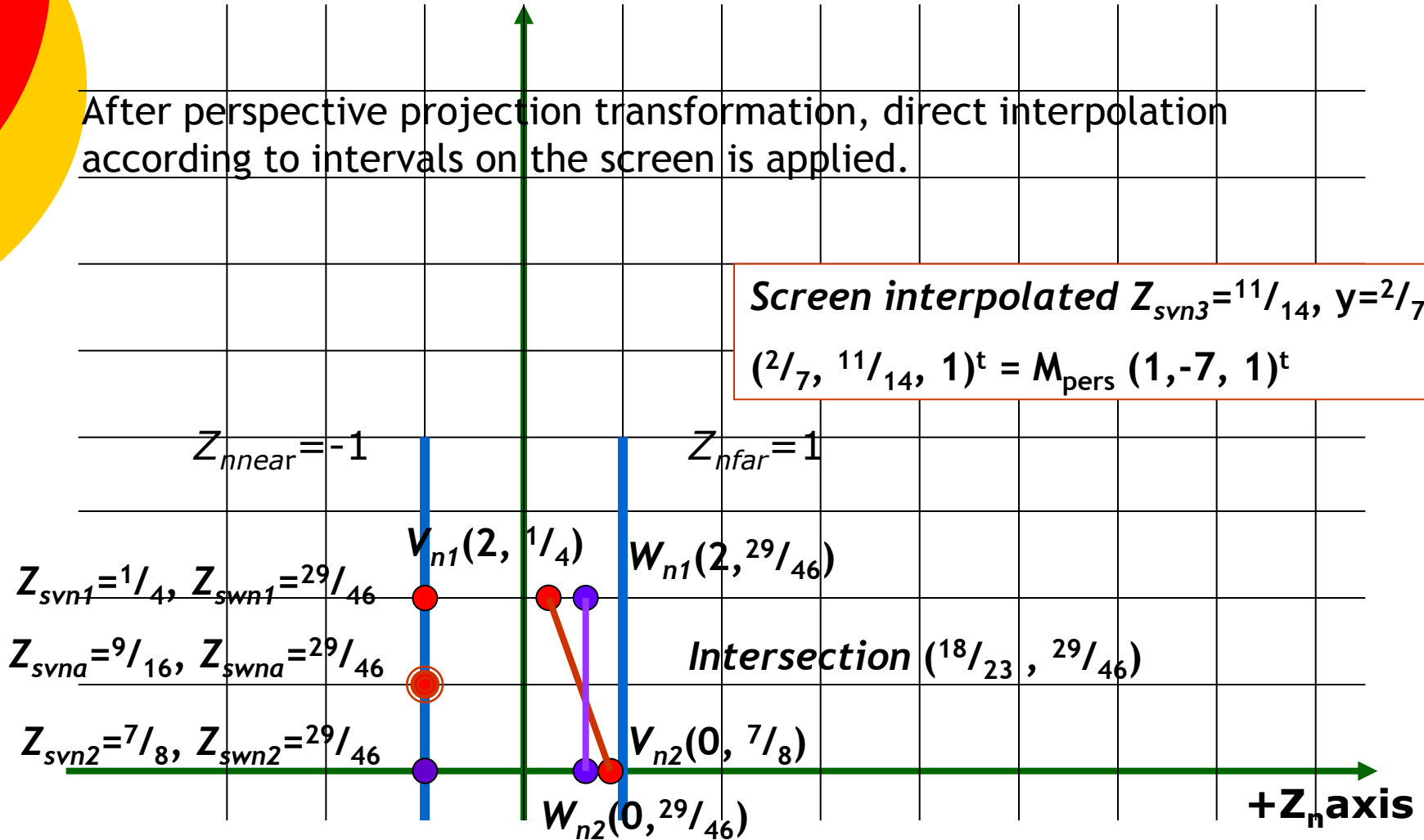
Perspective Projection Space

$$M_{pers} = \begin{bmatrix} -z_{near} & 0 & 0 & 0 \\ 0 & -z_{near} & 0 & 0 \\ 0 & 0 & \frac{z_{near} + z_{far}}{z_{near} - z_{far}} & \frac{-2z_{near}z_{far}}{z_{near} - z_{far}} \\ 0 & 0 & -1 & 0 \end{bmatrix}$$

Yaxis

After perspective projection transformation, direct interpolation according to intervals on the screen is applied.

Screen interpolated $Z_{svn3} = 11/14, y = 2/7;$
 $(2/7, 11/14, 1)^t = M_{pers} (1, -7, 1)^t$

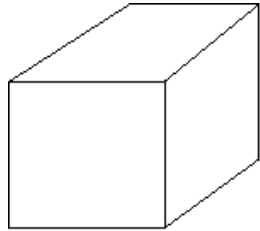




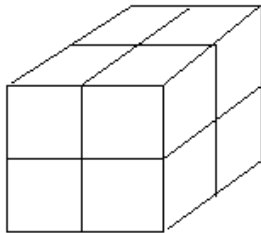
Space Partitioning

- Avoid rendering an object when it's unnecessary.
 - In many real-time applications, we want to eliminate as many objects as possible within the application.
 - Reduce burden on pipeline
 - Reduce traffic on bus
- Octree
- BSP tree

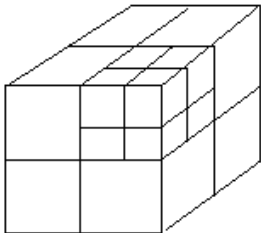
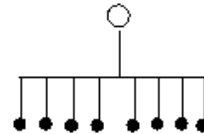
Octree



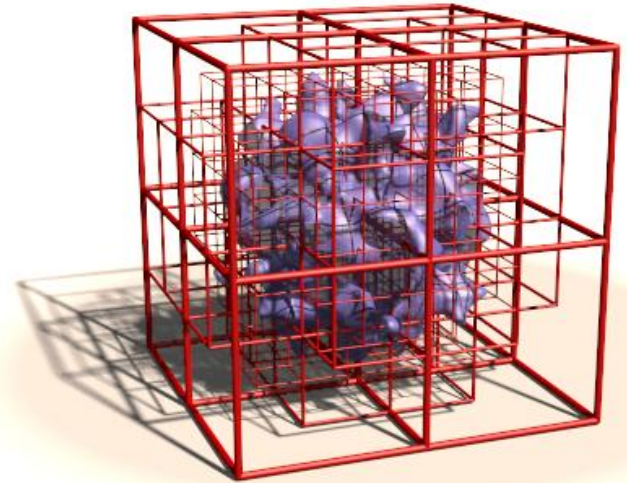
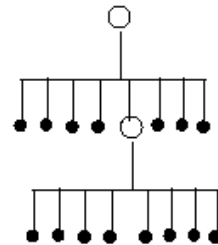
(root)



(1 level)



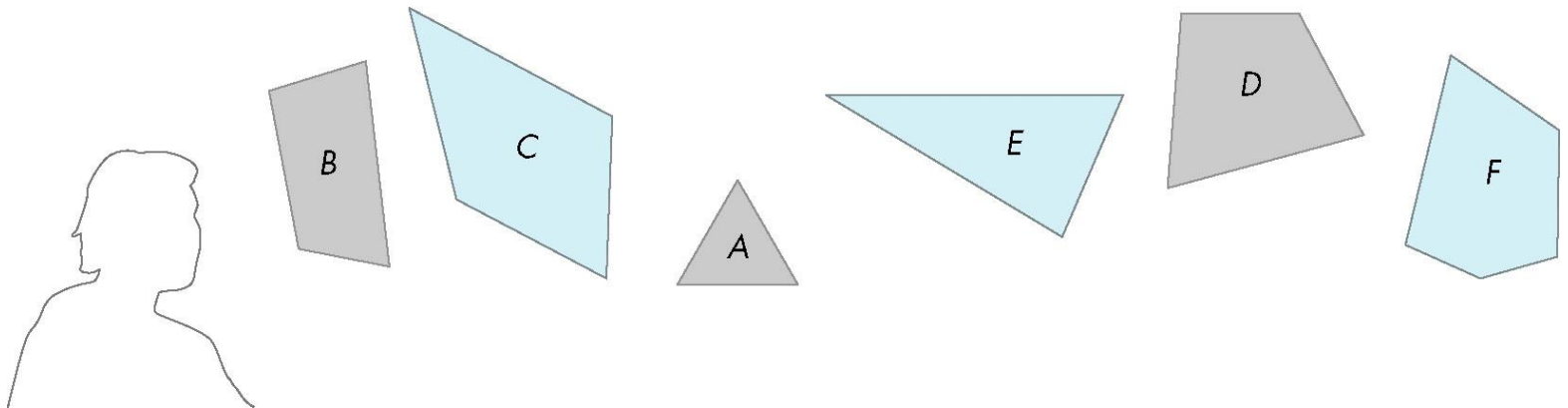
(2 levels)



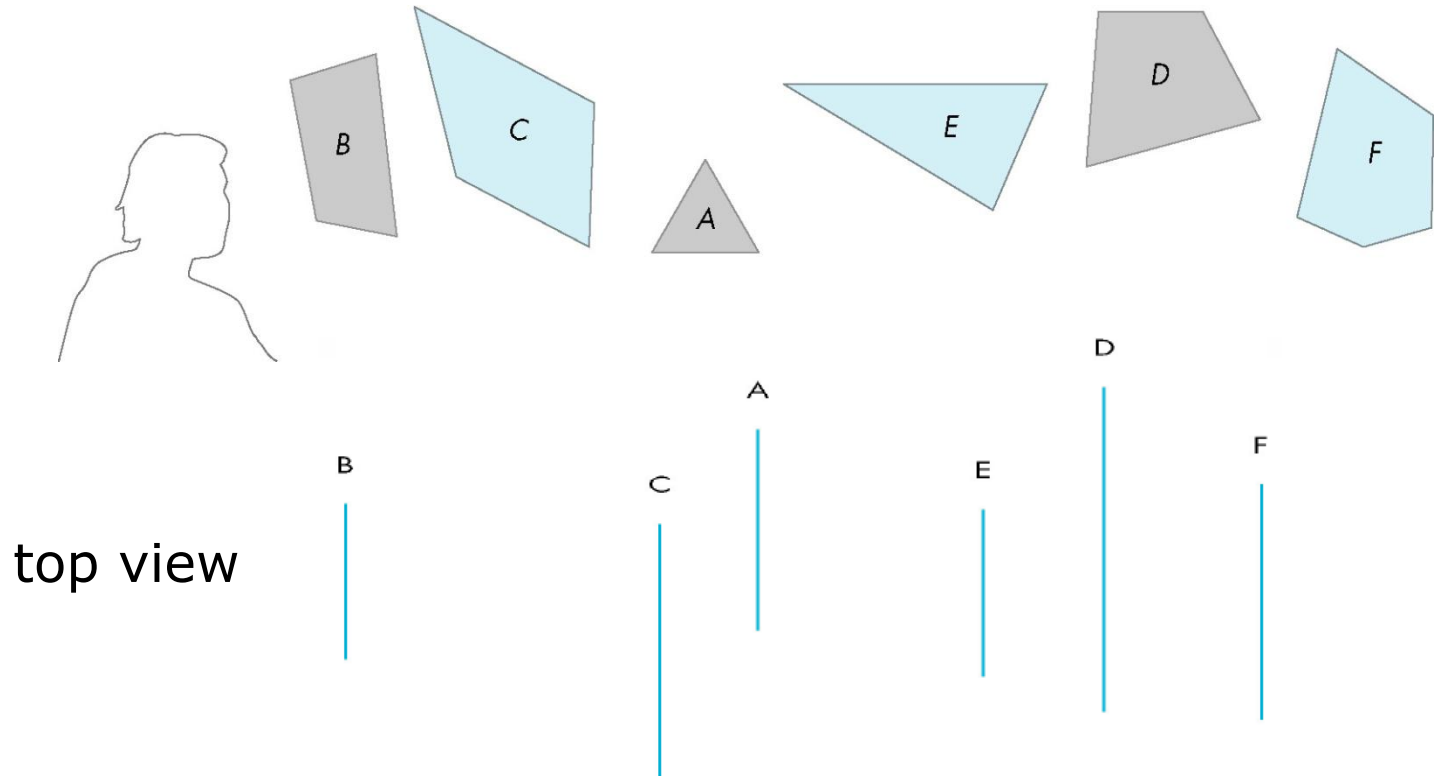
http://www.imagico.de/fast_iso/patch.html

Why do we use *BSP trees*?

- Hidden surface removal
 - A back-to-front painter's algorithm
- Partition space with Binary Spatial Partition (BSP) Tree



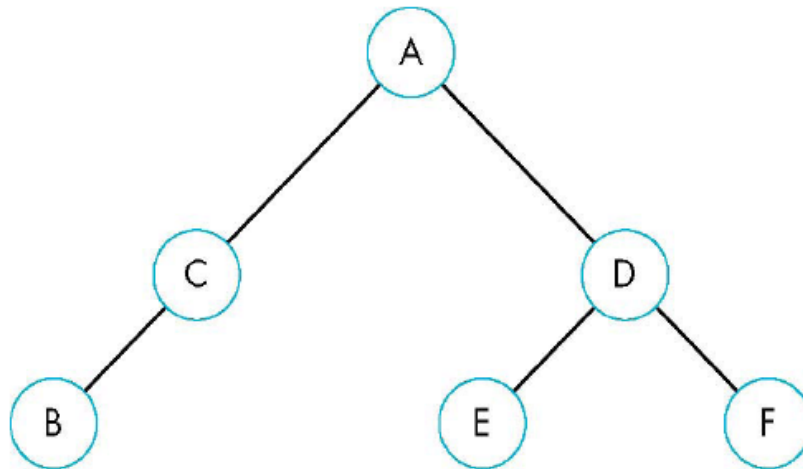
A Simple Example



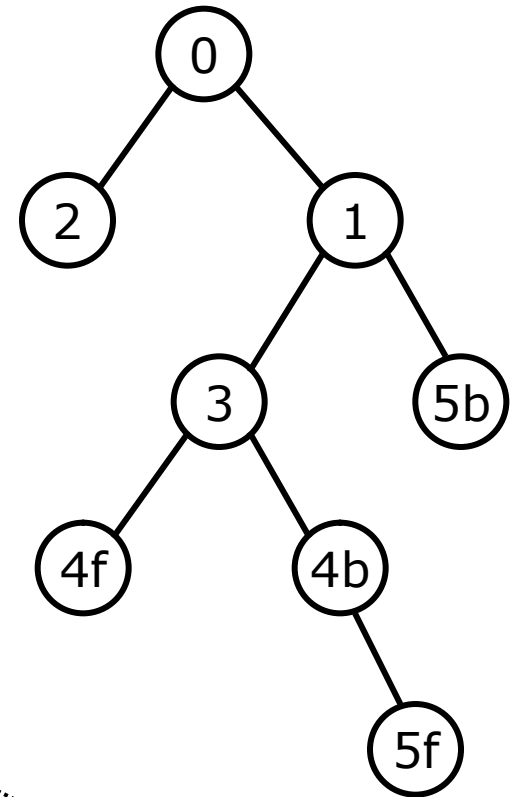
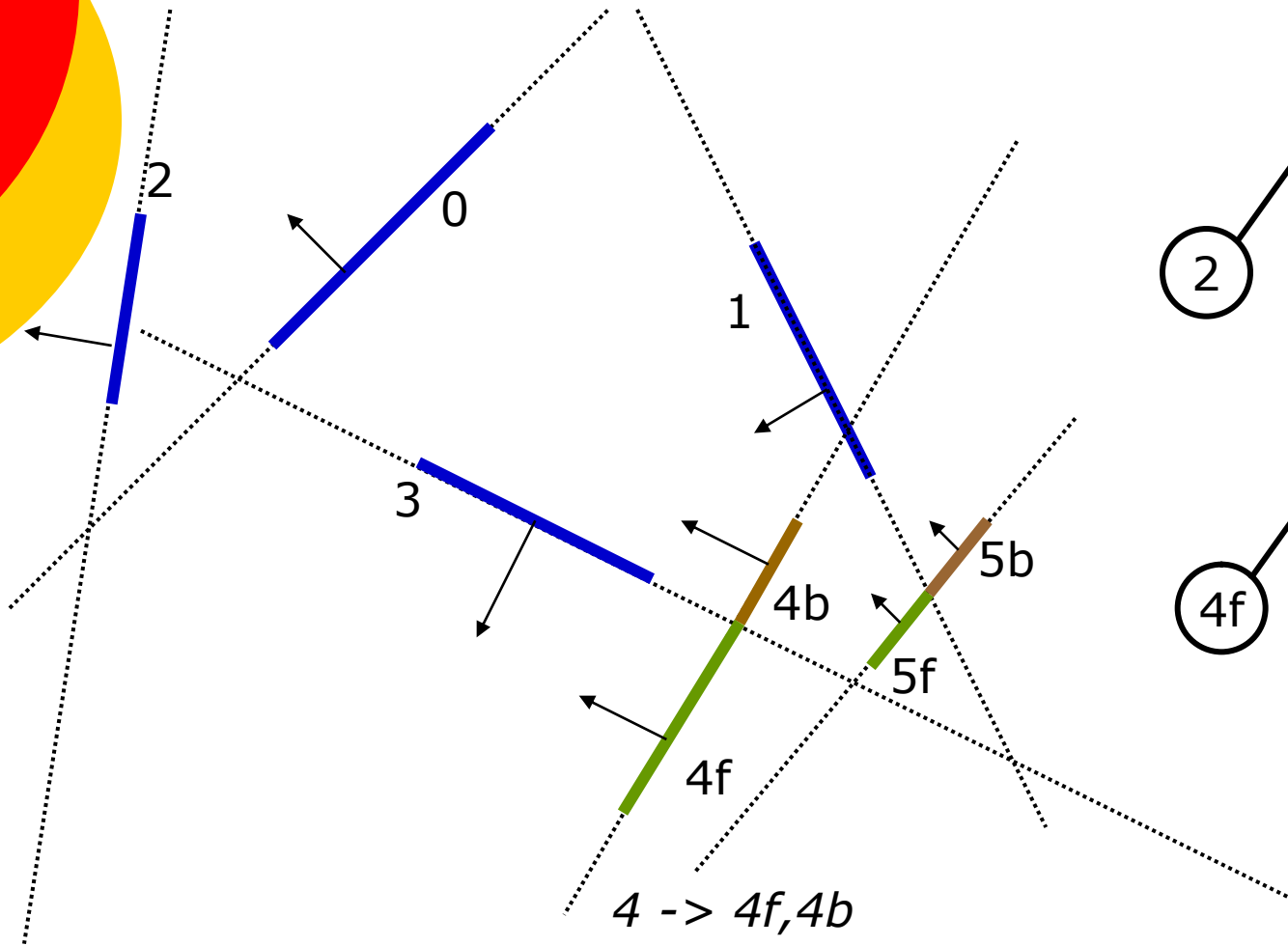
The plane of A separates B and C from D, E and F

Binary Space Partitioning Tree

- Can continue recursively
 - Plane of C separates B from A
 - Plane of D separates E and F
- Can put this information in a BSP tree
 - Use for visibility and occlusion testing



Creating a BSP tree

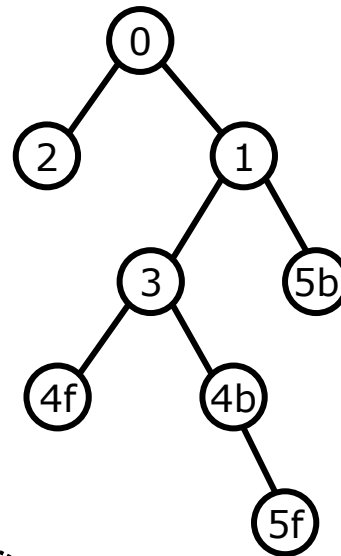
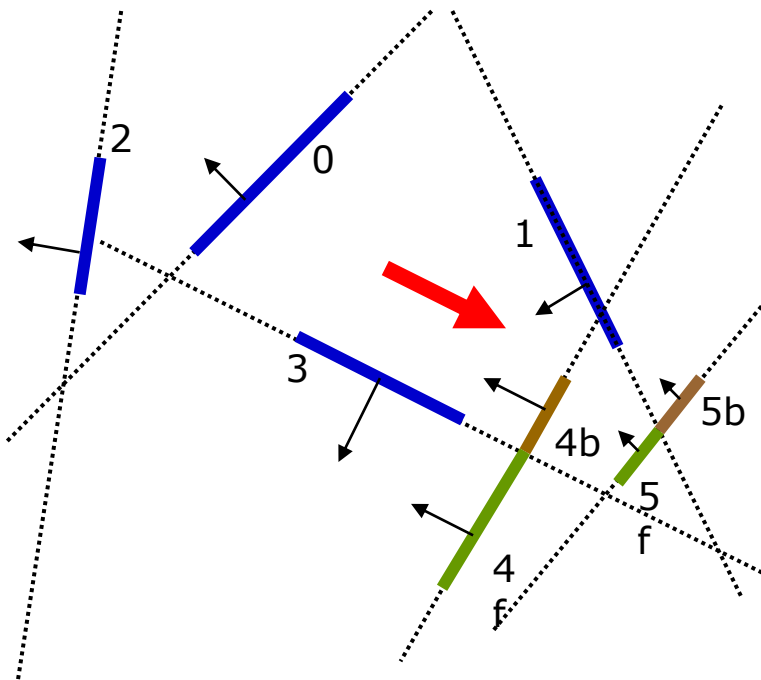
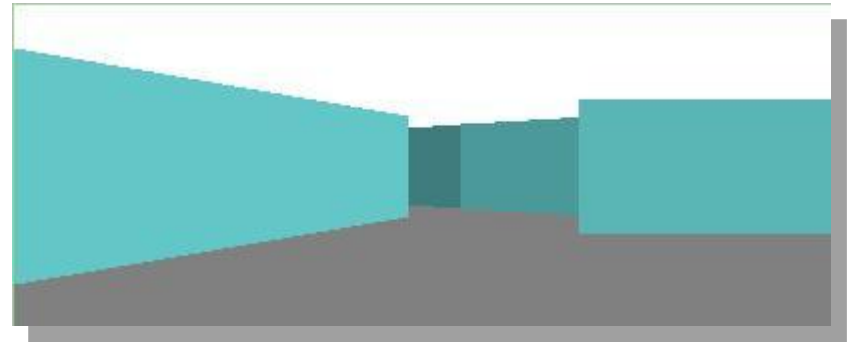




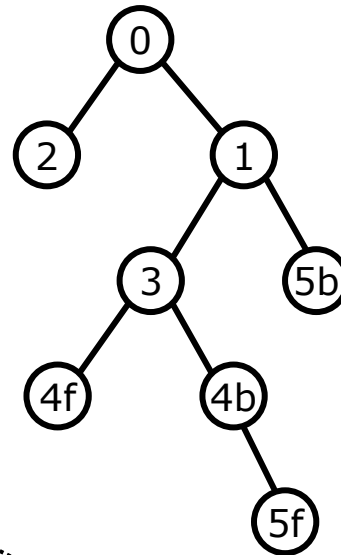
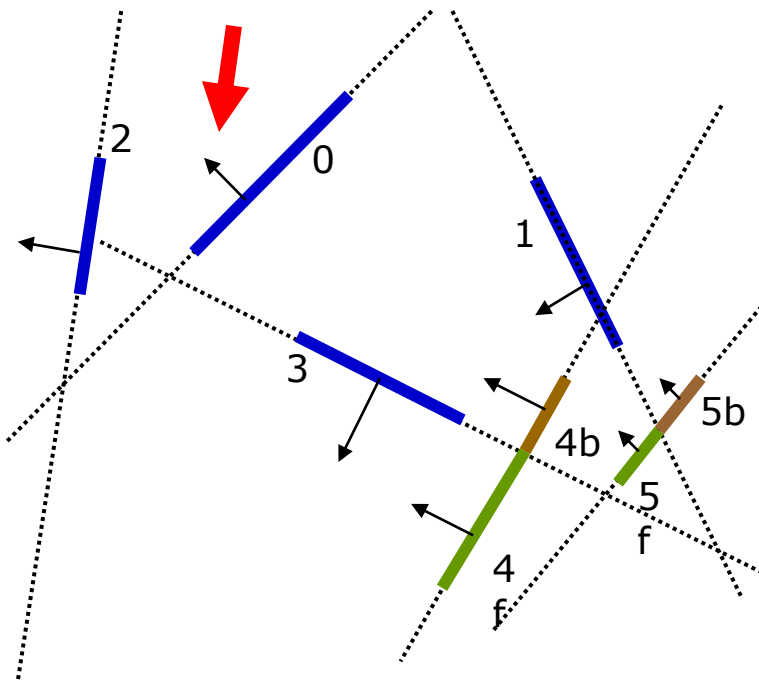
Back-to-Front Render

```
Render(node, view){
  if node is a leaf
    { draw this node to the screen }
  else
    if the viewpoint is in back of the dividing line
      {
        render(front subnode)
        draw node to screen
        render(back subnode)
      }
    else the viewpoint is in front of the dividing line
      {
        render (back subnode)
        draw node to screen
        render (front subnode)
      }
}
```

Back-to-Front Render



Back-to-Front Render



BSP-based Culling

- Pervasively used in first person shooting games.
 - Doom, quake....etc.
- Visibility test
- Skip objects that are “occluded”.



a screen shot from Doom.

Other Culling Tech.

- Portal Culling
 - Walking through architectures
 - Dividing space into cells
 - Cells only see other cells through portals

